COURSE PROFILE

| Course Name | Code | Semester | Term | Theory <br> +PS+Lab. <br> (hour/week) | Local Credits |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Introduction to Modern Algebra | MATH <br> 441 | Fall | 7 | $3+0+0$ | 3 |


| Prerequisites | None |
| :--- | :--- |


| Course Language | English |
| :---: | :---: |
| Course Type | Required |
| Course Lecturer |  |
| Course Assistant |  |
| Course Objectives | The aim of the course is to introduce students to the fundamentals of algebraic structures groups, rings, fields, and so forth. The students learn how to think mathematically, mathematical reasoning, using and handling with abstract mathematical objects and structures |
| Course Learning Outcomes | By the end of the course the students should be able to: <br> 1. to identify, compare, classify, justify, operate and apply the fundamental algebraic structures <br> 2. prepare for high-level mathematical courses <br> 3. to argue, create and formulate mathematical arguments and mathematical reasoning <br> 4. recognize the impact of abstract algebra on coding, cryptology and science <br> 5. recognize professional and ethical responsibilities of scientific writing |
| Course Content | Fundamentals: Sets, mappings, binary operations, relations, mathematical induction. Integers: Divisibility, prime factors, the greatest common divisor, congruence of integers and congruence classes. <br> Groups: Definition of a group, subgroups, cyclic groups, isomorphism, homomorphism, permutation groups, Cayley's theorem, normal subgroups, finite groups and Lagrange's theorem, quotient groups. <br> Rings, integral domains and fields: Definition of a ring, integral domains and fields, ideals and quotient rings, ring homomorphism. <br> Polynomials: Polynomials over a ring, divisibility of polynomials. |

## COURSE CONTENT

| Week | Subjects | Related Preparation |
| :--- | :--- | :--- |


| 1 | Binary Operation; Permutation and Inverses | Chapter 1 |
| :---: | :---: | :---: |
| 2 | Relations; Postulates for the integers; Mathematical Induction | Chapter 2 |
| 3 | Divisibility; Prime Factors and the Greatest Common Divisor | Chapter 2 |
| 4 | Congruence of Integers; Congruence Classes | Chapter 2 |
| 5 | Definition of a Group; | Chapter 3 |
| 6 | Subgroups; Cyclic Groups | Chapter 3 |
| 7 | Isomorphisms; Homomorphisms | Chapter 3 |
| 8 | Finite Permutation Groups; Cayley's Theorem | Chapter 4 |
| 9 | Normal Subgroups | Chapter 4 |
| 10 | Quotient Groups | Chapter 4 |
| 11 | Definition of a Ring; Integral Domains and Fields | Chapter 5 |
| 12 | Ideals and Quotient Rings; Ring Homomorphisms | Chapter 6 |
| 13 | Polynomials over a Ring; | Chapter 8 |
| 14 | Divisibility and the Greatest Common Divisor; | Chapter 8 |


| Course Textbooks | J. Gilbert and L. Gilbert: Elements of Modern Algebra, sixth Edition, Thomson. |
| :--- | :--- |
| Recommended <br> References | I.N. Herstein, Abstract Algebra, Prentice-Hall. |
| J.B. Fraleigh, Abstract Algebra, Addison-Wesley. |  |


| Semester Requirements | Number | Percentage of Grade |
| :--- | :--- | :--- |
| Attendance/Participation | 1 | 10 |
| Laboratory | - | - |
| Application | - | - |


| Special Course Internship (Work Placement) | - | - |
| :---: | :---: | :---: |
| Quizzes/Studio Critics | - | - |
| Homework Assignments | 13 | - |
| Presentation | - | - |
| Project | - | - |
| Seminar/Workshop | - | - |
| Midterms/Oral Exams | 2 | 60 |
| Final/Resit Exam | 1 | 30 |
| Total | 17 | 100 |


| PERCENTAGE OF SEMESTER WORK | 16 | 70 |
| :--- | :--- | :--- |
| PERCENTAGE OF FINAL WORK | 1 | 30 |
| Total | 17 | 100 |


| Course Category | Core Courses |  |
| :--- | :--- | :--- |
|  | Major Area Courses |  |
|  | Supportive Courses | . |
|  | Media and Managment Skills Courses |  |
|  | Transferable Skill Courses |  |
|  |  |  |

## COURSE'S CONTRIBUTION TO PROGRAM

| \# | Program Qualifications / Outcomes | * Level of Contribution |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
| 1 | To have a grasp of basic mathematics, applied mathematics and theories and applications of statistics. |  |  |  | X |  |
| 2 | To be able to use theoretical and applied knowledge acquired in the advanced fields of mathematics and statistics, |  |  |  |  | X |
| 3 | To be able to define and analyze problems and to find solutions based on scientific methods, |  |  |  |  | X |
| 4 | To be able to apply mathematics and statistics in real life with interdisciplinary approach |  |  |  |  | X |


|  | and to discover their potentials, |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 5 | To be able to acquire necessary information and to make modeling in any field that mathematics is used and to improve herself/himself, |  |  | X |
| 6 | To be able to criticize and renew her/his own models and solutions, |  |  | X |
| 7 | To be able to tell theoretical and technical information easily to both experts in detail and nonexperts in basic and comprehensible way, |  | X |  |
| 8 | To be able to use international resources in English and in a second foreign language from the European Language Portfolio (at the level of B1) effectively and to keep knowledge up-to-date, to communicate comfortably with colleagues from Turkey and other countries, to follow periodic literature, |  | X |  |
| 9 | To be familiar with computer programs used in the fields of mathematics and statistics and to be able to use at least one of them effectively at the European Computer Driving Licence Advanced Level, | X |  |  |
| 10 | To be able to behave in accordance with social, scientific and ethical values in each step of the projects involved and to be able to introduce and apply projects in terms of civic engagement, |  | X |  |
| 11 | To be able to evaluate all processes effectively and to have enough awareness about quality management by being conscious and having intellectual background in the universal sense, |  | X |  |
| 12 | By having a way of abstract thinking, to be able to connect concrete events and to transfer solutions, to be able to design experiments, collect data, and analyze results by scientific methods and to interfere, |  |  | X |
| 13 | To be able to continue lifelong learning by renewing the knowledge, the abilities and the compentencies which have been developed during the program, and being conscious about lifelong learning, |  | X |  |
| 14 | To be able to adapt and transfer the knowledge gained in the areas of mathematics and statistics to the level of secondary school, |  | X |  |
| 15 | To be able to conduct a research either as an individual or as a team member, and to be effective in each related step of the project, to take role in the decision process, to plan and manage the project by using time effectively. |  | X |  |

*1 Lowest, 2 Low, 3 Average, 4 High, 5 Highest
ECTS ALLOCATED BASED ON STUDENT WORKLOAD BY THE COURSE DESCRIPTION

| Activities | Number | Duration (Hours) | Total Workload |
| :--- | :--- | :--- | :--- | :--- |


| Course Hours (Including Exams) | 14 | 3 | 48 |
| :---: | :---: | :---: | :---: |
| Tutorials | - | - | - |
| Laboratory | - | - | - |
| Application | - | - | - |
| Special Course Internship (Work Placement) | - | - | - |
| Field Work | - | - | - |
| Study Hours Out of Class | 14 | 4 | 56 |
| Presentations / Seminar | - | - | - |
| Project | - | - | - |
| Preparatory reading | 13 | 2 | 26 |
| Homework Assignments | 13 | 4 | 52 |
| Quizzes | - | - | - |
| Midterm Exams | 2 | 4 | 8 |
| Final / Resit Exam | 1 | 10 | 10 |
|  |  | Total Workload | 200 |

COURSE CATEGORY
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\begin{array}{|l|l|l|l|l|}\hline \begin{array}{l}\text { ISCED } \\
\text { GENERAL } \\
\text { AREA } \\
\text { CODES }\end{array}
$$ \& GENERAL AREAS \& ISCED <br>
BASIC AREA <br>

CODES\end{array}\right)\) BASIC EDUCATIONAL AREAS |  |
| :--- |
| 1 |


| 4 | Science | 44 | Natural Sciences | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 4 | Science | 46 | Mathematics and Statistics | 100 |
| 4 | Science | 48 | Computer | 0 |
| 5 | Engineering, Manufacturing and Civil | 52 | Engineering | 0 |
| 5 | Engineering, Manufacturing and Civil | 58 | Architecture and Structure | 0 |
| 5 | Agriculture | Manufacturing and Processing | 0 |  |
| 6 | Medicine and Welfare | Manura, Forestry, Livestock, Fishery | 0 |  |
| 7 | Medicine and Welfare | Serving and Civil | 54 | Medical |
| 7 | Service | 76 | Social Services | 0 |
| 8 | Service | Personal Services | 0 |  |
| 8 | Sransport Services | 0 | 0 |  |
| 8 | 84 | Environment Protection | 0 |  |

